Bioinformatics Software Lab Introduction to Analysis of Single Cell Sequencing

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Objectives

- 1. basics of single cell sequencing
- 2. basic bioinformatics/computational problems
 - dimension reduction
 - clustering
 - data integration

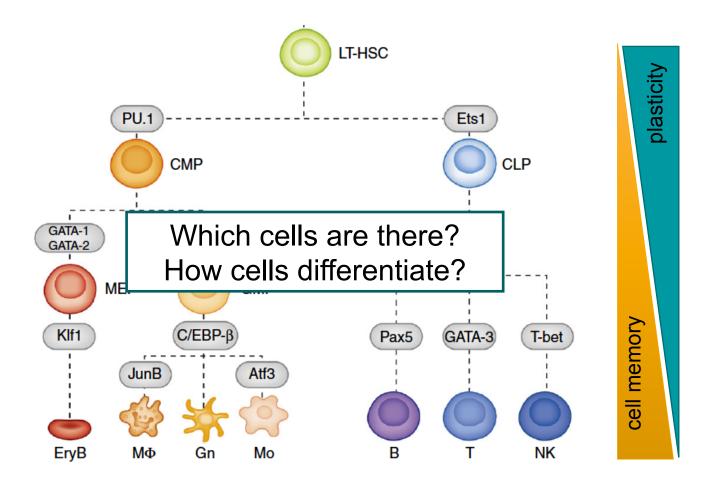


Expression at Single Cell Level

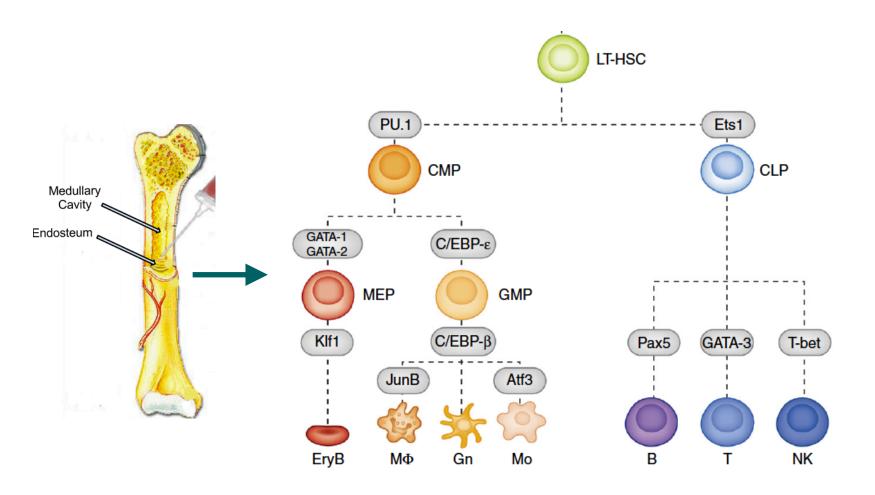


Cell Differentiation

Hematopoiesis

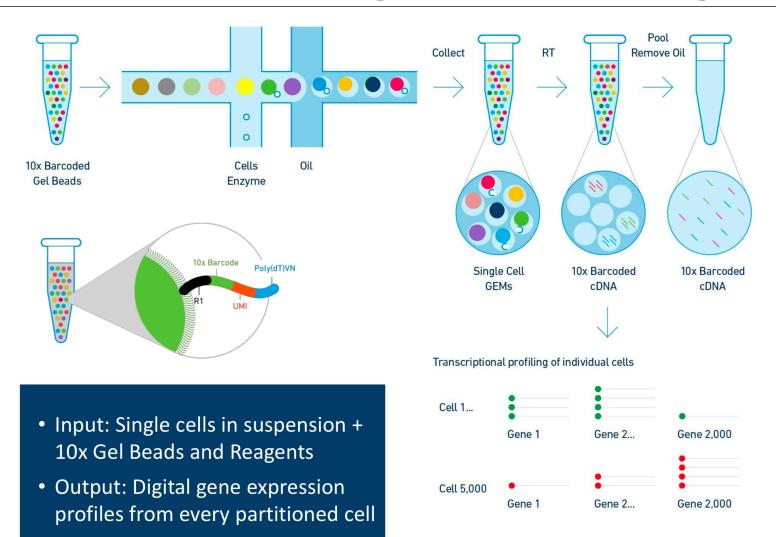


Cell Differentiation



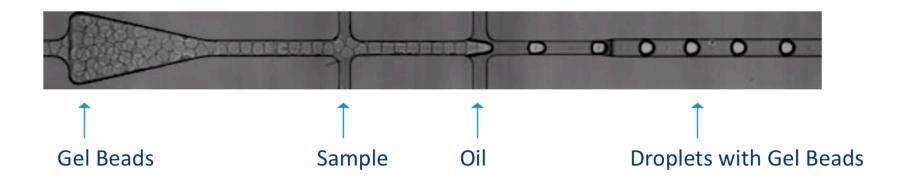
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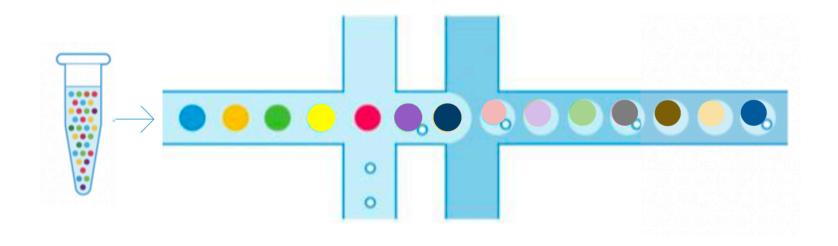
Droplet based RNA single cell sequencing



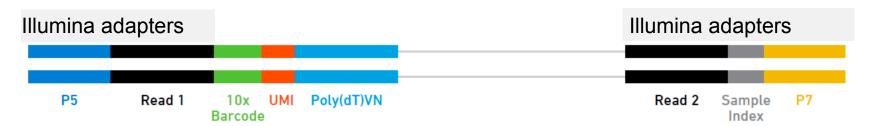


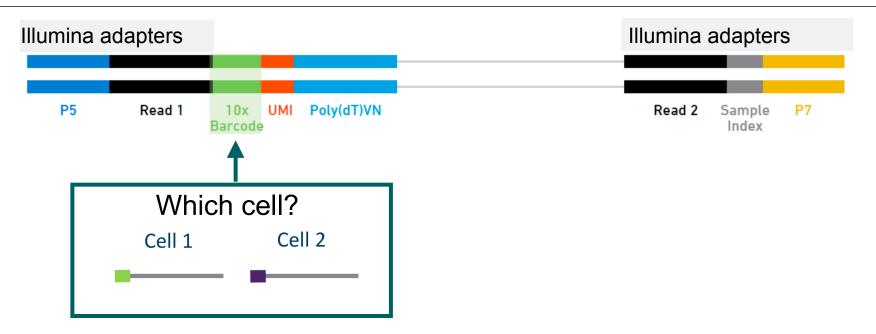
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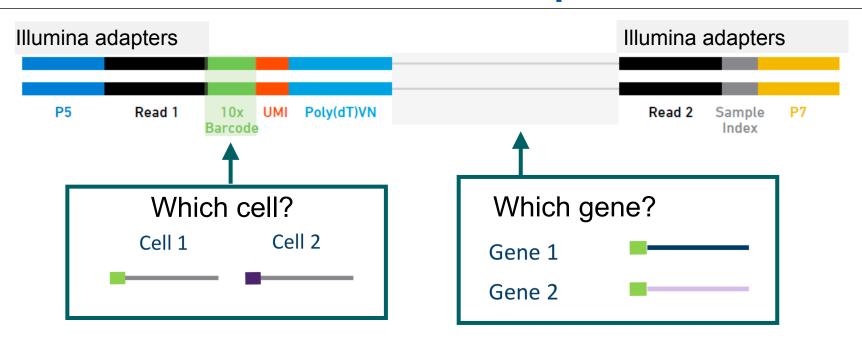


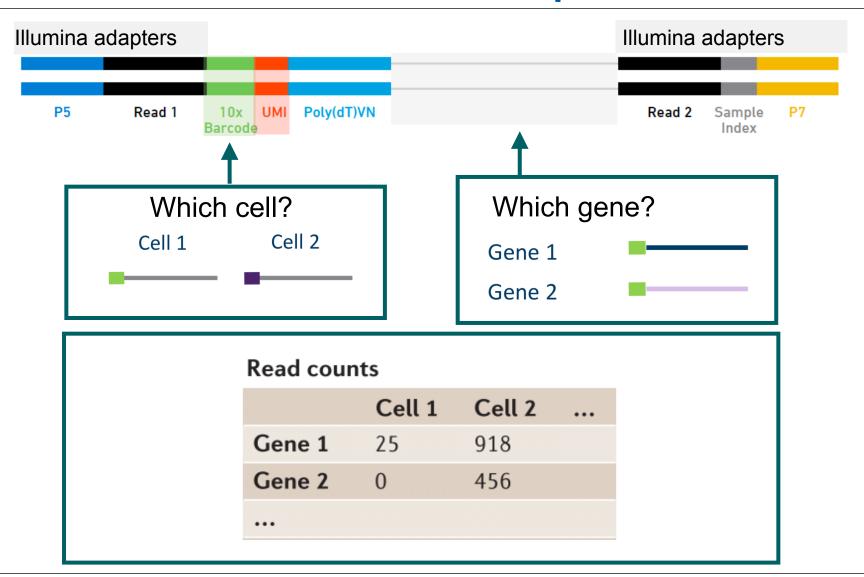






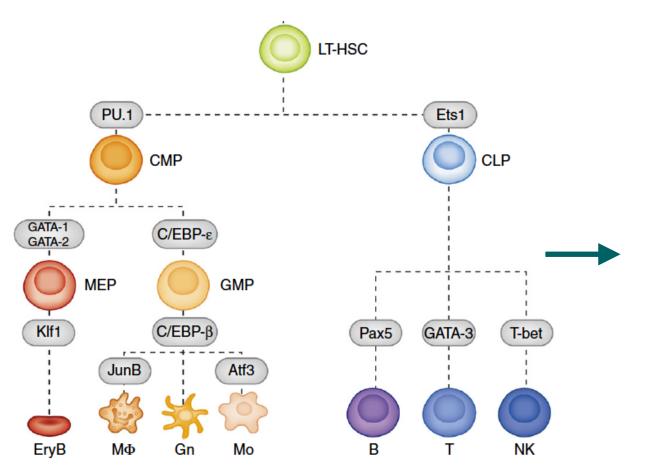








Cell Differentiation & Gene Expression

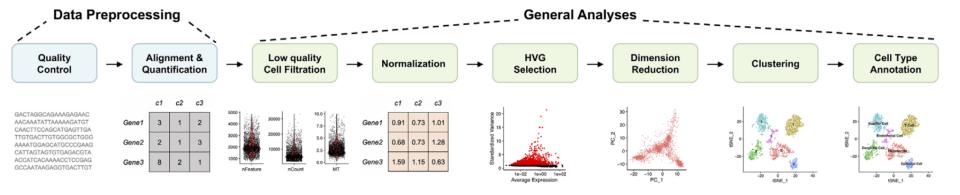


	Cell 1	Cell 2	
Gene 1	25	918	
Gene 2	0	456	
Gene 3	20	342	
Gene 4	0	214	

Source: Amit (2016), Nature Immunoloy.

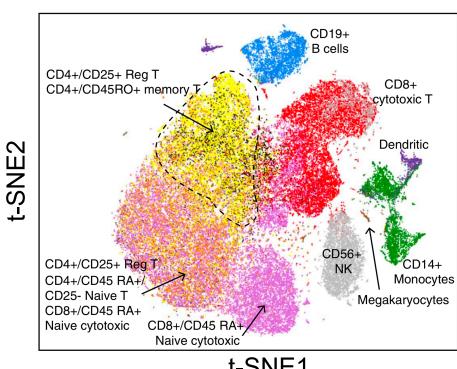


Basics Bioinformatics - single cell RNA-seq



Gene Expression of Lymphoid Cells

PBMCs from Humans

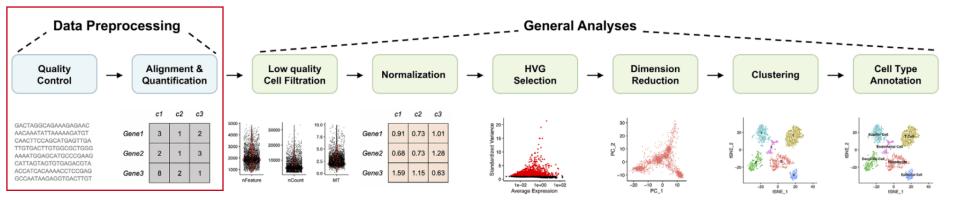


t-SNE1

Single cell RNA-seq from 68k cells

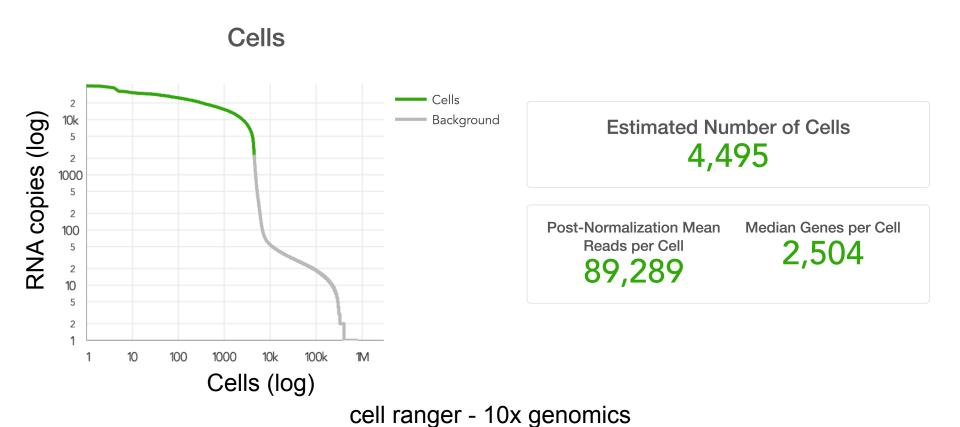
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Basics Bioinformatics - single cell RNA-seq



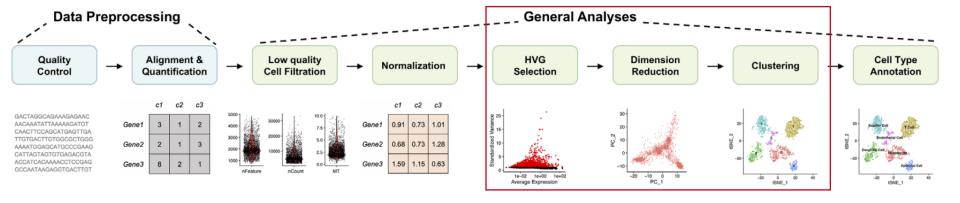
Basics Bioinformatics - Cell Filtering

- 1. sum UMIs (copy of transcripts) per cell
- 2. consider cells with total UMI count > 99th of expected recovered cells





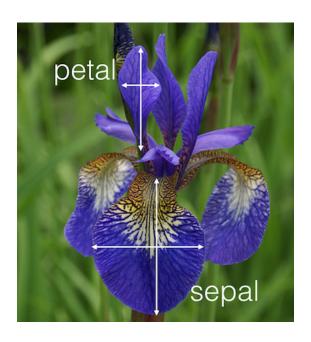
Basics Bioinformatics - single cell RNA-seq



Clustering & Dimension reduction



- Given a data description
 - i.e. measurement of size of iris flowers
- Find groups of similar observations
 - i.e. iris flower sub-types

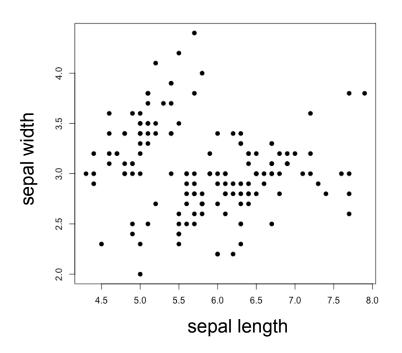


	Sepal Length	Sepal Width	Petal Length	Petal Width
Flower 1	5.1	3.5	1.4	0.2
Flower 2	4.9	3.0	1.4	0.2
Flower 3	4.7	3.2	1.3	0.2
Flower 4	4.6	3.1	1.5	0.2



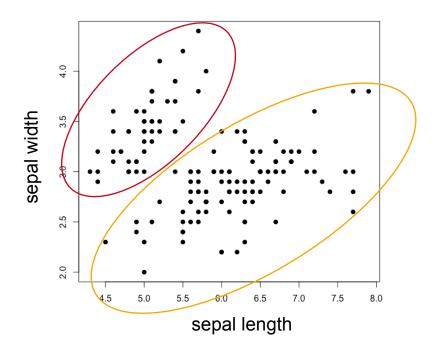
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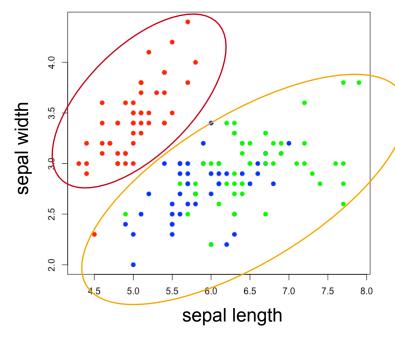
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Iris Setosa





Iris Virginia



Iris Versicolor



Clustering Formalism

For a given data:

 Matrix X with N observations and L dimensions where x_i is a vector representing observation i

X11	X12		X1L
X21	X22	•••	X 2L
X 31	X 32		X 3L
X _{N1}	X _{N2}		XNL

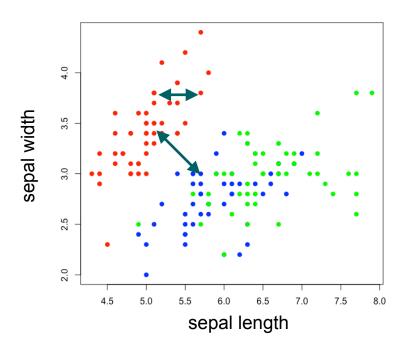
find groups of similar observations

• vector $Y = (y_1, ..., y_N)$ where $y_i \in \{1, ..., K\}$ indicates the cluster of observation i



Distance

- A important concept in clustering is a distance (similarity)
 between a pair of objects x_i and x_j
 - Observations of a same group should be close in space

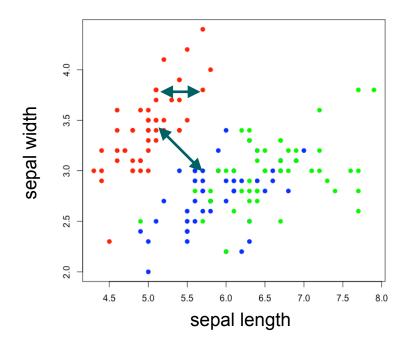


Euclidean distance (sensitive to scale)

$$d(x_i, x_j) = \sqrt{\sum_{l=1}^{L} (x_{il} - x_{jl})^2}$$

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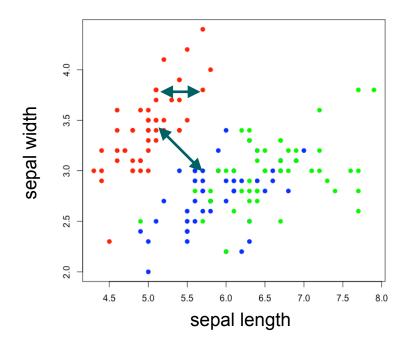
Pearson Correlation (scale insensitive/ similarity)

$$d(x_i, x_j) = \frac{\sum_{l=1}^{L} (x_{il} - \overline{x}_i)(x_{jl} - \overline{x}_j)}{\sigma_i^2 \sigma_j^2}$$



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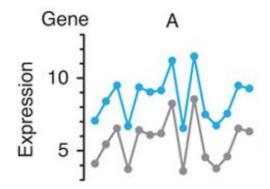
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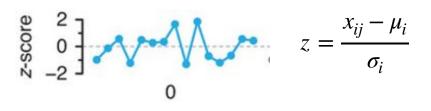
Distance and Scale

- In some problems scale can be important!
 - Similarly in changes are more important / not absolute values.

unscaled data



Euclidean - not similar Correlation - similar z-score normalised data



Euclidean - similar Correlation - similar

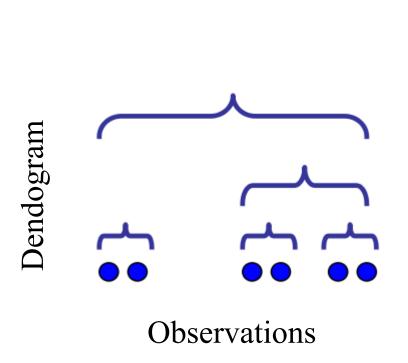


Clustering Methods

Hierarchical methods

- Mostly bottom up
- based on distance / simple to interpret
- Partitional methods (k-means or mixture models)
 - Mostly top down
 - Use models of groups, centroids
- Graph based methods
 - Use graph formalisms to represent data:
 - nodes are objects
 - edges weights represent similarities
 - find well connected graphs



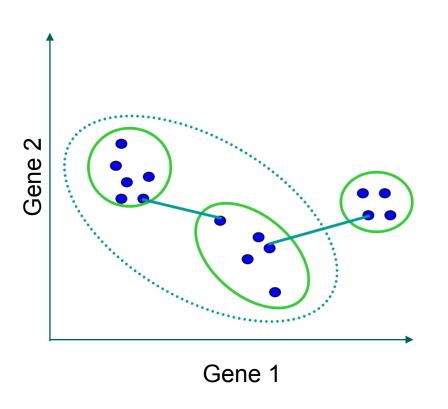


- Botton up method
- Starting with a distance (similarity) matrix and each object as a group

Repeat:

- Joint two most similar groups
- Until the dendrogram has only one group





Single-Linkage

- Join two groups where two examples are close
- Find groups with linear shapes



Distance Matrix







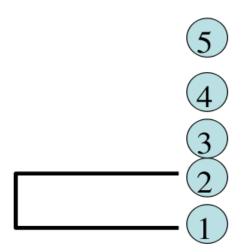






Distance Matrix

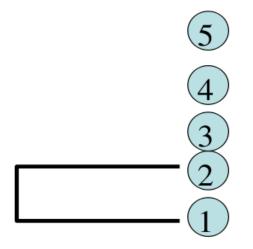
	1 2	2 3	3 4	1 5	5
1	0				7
1 2 3 4 5	2	0			
3	6 10 9	3	0		
4	10	9	/	0	
5	9	8	5	4	0





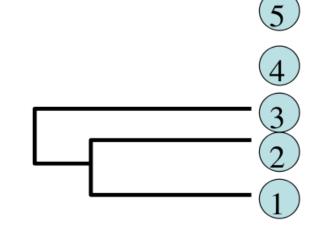
Distance Matrix

$$\begin{aligned} d_{(1,2),3} &= \min\{d_{1,3}, d_{2,3}\} = \min\{6,3\} = 3\\ d_{(1,2),4} &= \min\{d_{1,4}, d_{2,4}\} = \min\{10,9\} = 9\\ d_{(1,2),5} &= \min\{d_{1,5}, d_{2,5}\} = \min\{9,8\} = 8 \end{aligned}$$



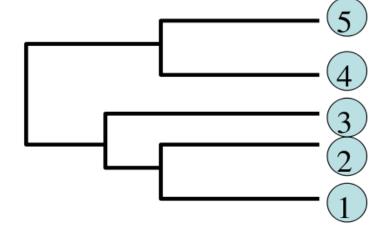


$$\begin{aligned} d_{(1,2,3),4} &= \min\{d_{(1,2),4}, d_{3,4}\} = \min\{9,7\} = 7 \\ d_{(1,2,3),5} &= \min\{d_{(1,2),5}, d_{3,5}\} = \min\{8,5\} = 5 \end{aligned}$$

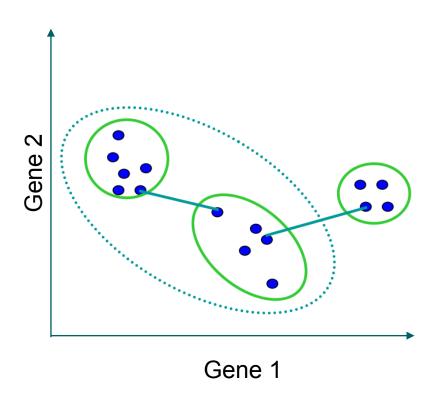




$$d_{(1,2,3),(4,5)} = \min\{d_{(1,2,3),4},d_{(1,2,3),5}\} = 5$$







Single-Linkage

- Groups with closest genes
- linear shapes

Complete-Linkage

- Closest groups with more far genes
- Compact clusters

Average Linkage

- Groups with closest centroids (middle)
- Outlier robust



Hierarchical Clustering

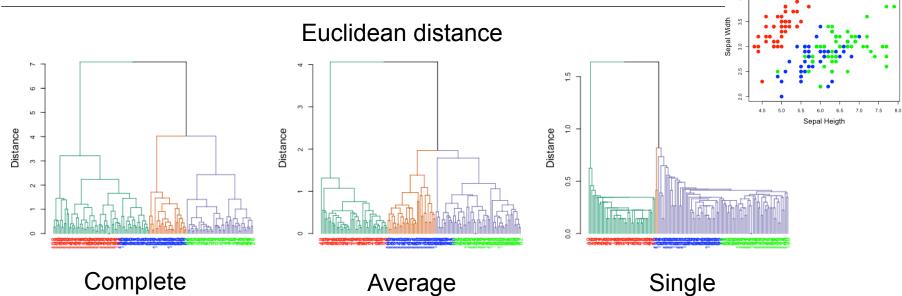
Which linkage?

Which distance?



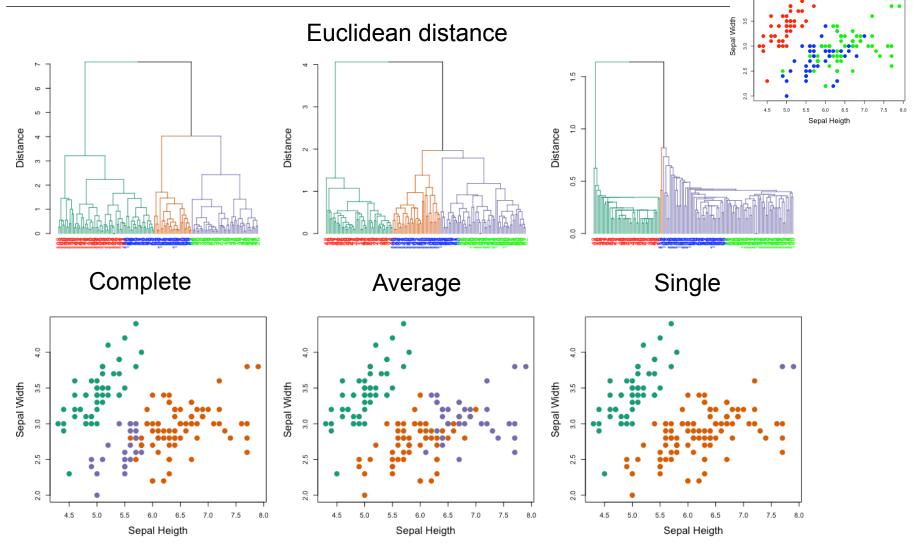
True labels

Hierarchical Clustering of Iris



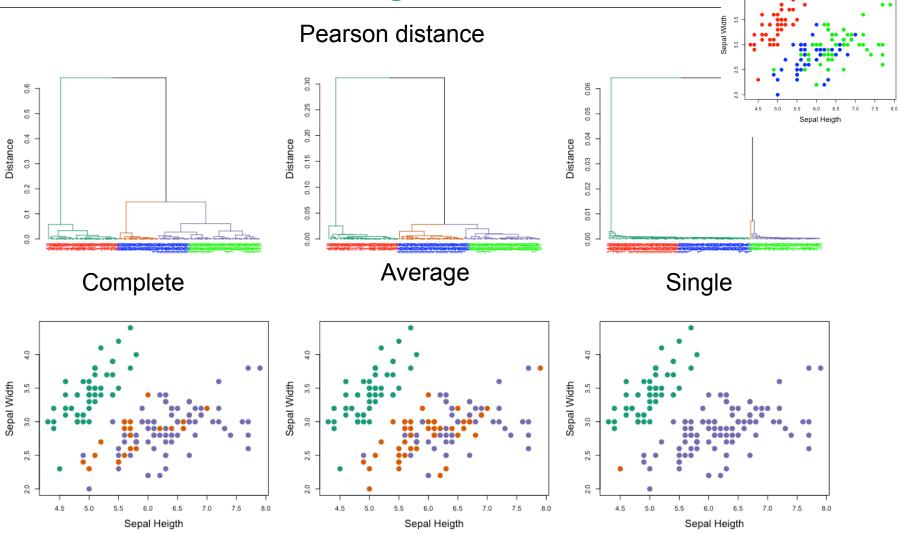
True labels

Hierarchical Clustering of Iris





Hierarchical Clustering of Iris



- · Hierarchical cluster is sensitive to noise/outliers
- High computational cost O(n²)



True labels

K-means

Iterative algorithm using **centroids** as cluster representations

Requires specification of number of clusters (K)

Algorithm:

Start cluster (Y) randomly

Repeat for a number of iterations

- estimate centroid (m_k) for each cluster

$$m_k = \frac{\sum_{i=1}^{N} 1(y_i = k) x_i}{\sum_{i=1}^{N} 1(y_i = k)}$$

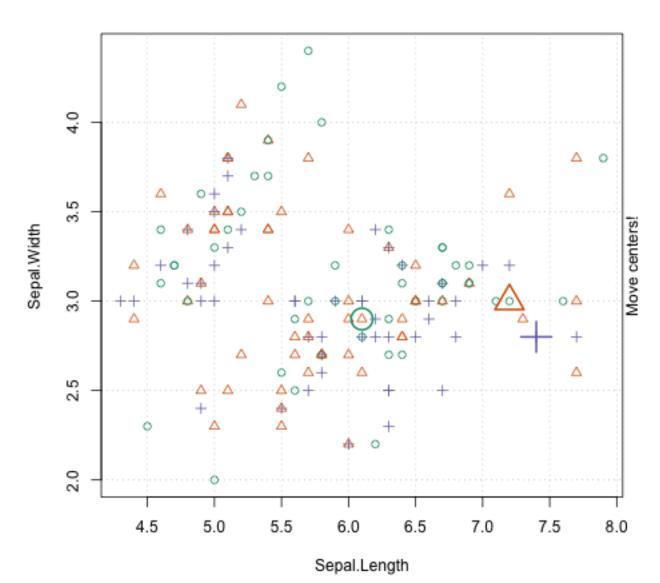
Assign objects to closest centroid:

$$y_i = \operatorname{argmin}_k \operatorname{d}(x_i, m_k)$$

^{*} convergence is only guaranteed for Euclidean distance

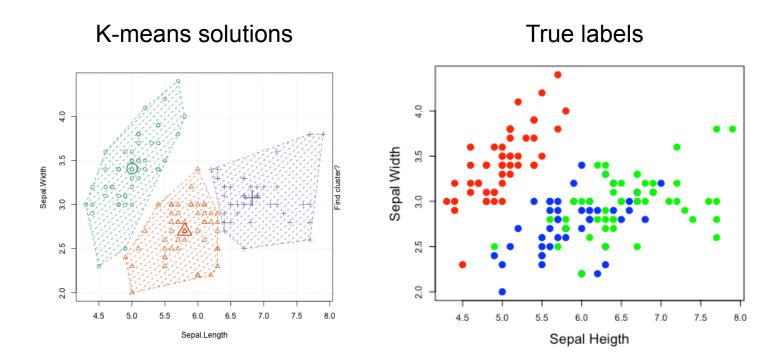


K-means on Iris





K-means on Iris

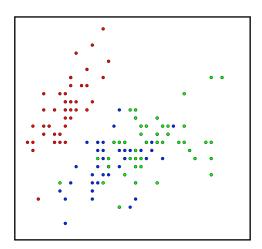


- K-means tends to find spherical clusters
- Sensitive to initialisation

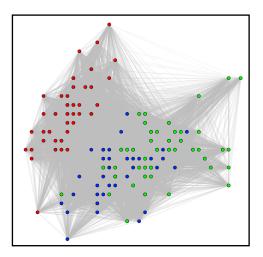


• data points are nodes



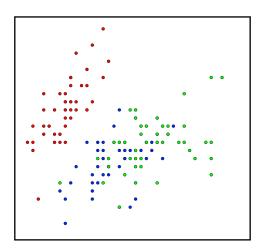


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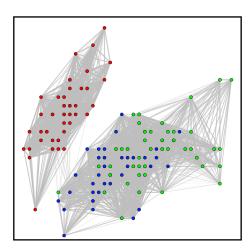


• edges represent similarities

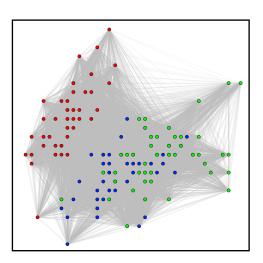




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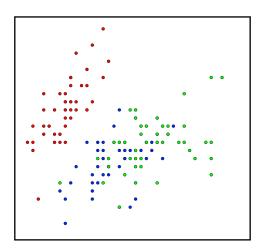


 k-nearest neighbours (KNN) -> sparse graphs

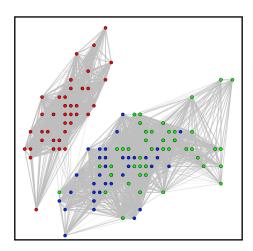


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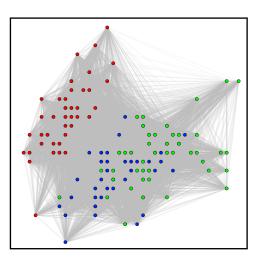




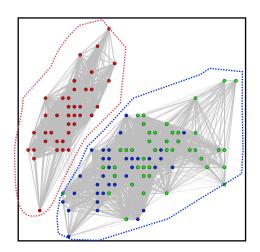
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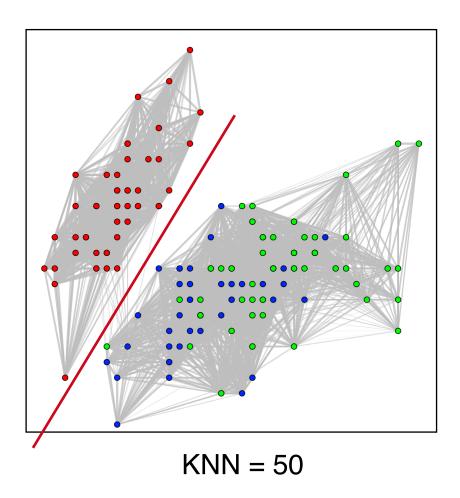
edges represent similarities



• find well connected sub-graphs

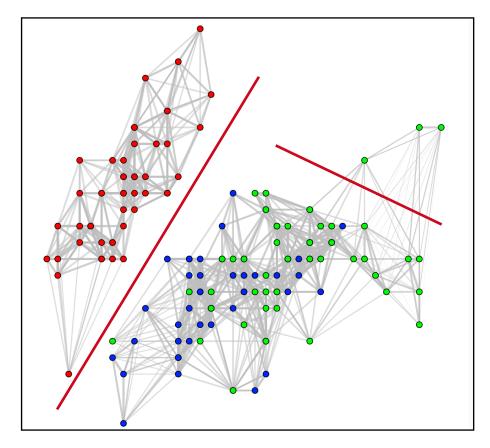


Graph cut



- Cluster by finding cuts in the graph
- Cut cost C(A,B) = sum of edge weights in cut

Graph cut

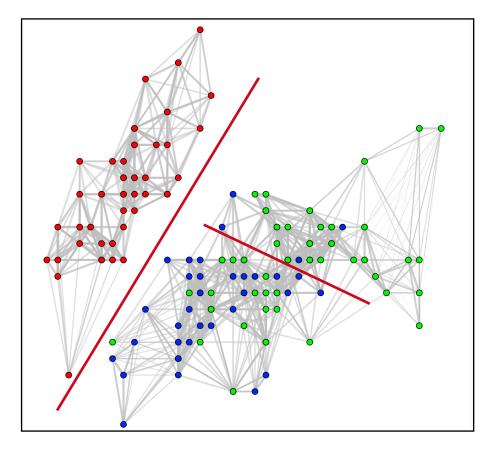


KNN = 10

- Cluster by finding cuts in the graph
- Cut cost C(A,B) = sum of edge weights in cut
 - smallest cuts might not be the best



Normalized graph cut



KNN = 10

 Normalized graph cut avoids small graphs

$$normCUT(A,B) = \frac{CUT(A,B)}{VOL(A)} + \frac{CUT(A,B)}{VOL(B)}$$

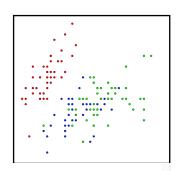
where VOL(A) is the weight sums of cluster A.

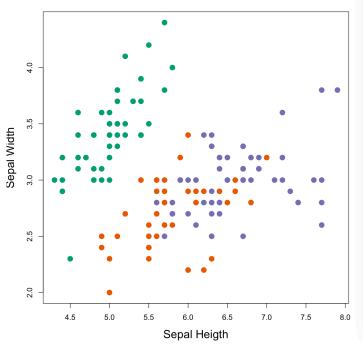


Spectral Clustering

From a graph weight matrix *W* derived from a (i.e. KNN or kernel function)

- 1. Estimate the laplacian L=D-W where D is a diag. matrix $d_{ii} = \sum w_{ij}$
- 2. Estimate eigenvalues of *L*
- 3. Perform *k*-means on lowest K eigenvalues
- spectral clustering is equivalent to find normCUT in graphs
- eigenvalues equal to 0 represent connected graphs
- graph sparsity (KNN) makes spectral clustering efficient for large n







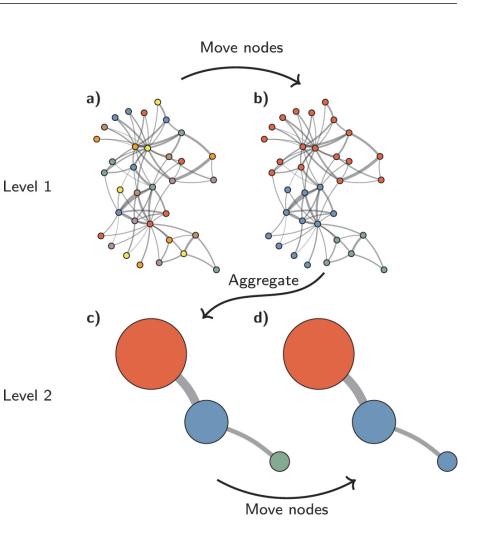
Single cell Clustering Methods / Leiden algorithm

Optimize cluster modularity

$$\mathcal{H} = \sum_{c} [e_c - \gamma(\frac{n_c}{2})],$$

where n_c is the size of cluster and e_c is the number of expected edges

- A) Start with singleton partition
- B) Move nodes improving H
- C) Create a meta-graph level
- D) Move nodes improving H



Institute for



Resume / Clustering Methods

- · K-means, hierarchical clustering, spectral clustering
 - standard algorithms with standard performance on simple clustering problems
- Clustering of single cell algorithms
 - Leiden and louvain clustering
 - Robust and scale well to large data sets
- Further issues:
 - Data dimensionality:
 - distances do not work well on high dimension
 - visualisation is easier in low level space
 - Validation:
 - How many clusters is present in the data?
 - Which is the best method?

More details on clustering

- Hastie, Tibshirani and Friedman, The Elements of Statistical Learning, Chapter 14 Corr
- Video lecture: https://www.youtube.com/watch?v=Qa6k7Rlwltg



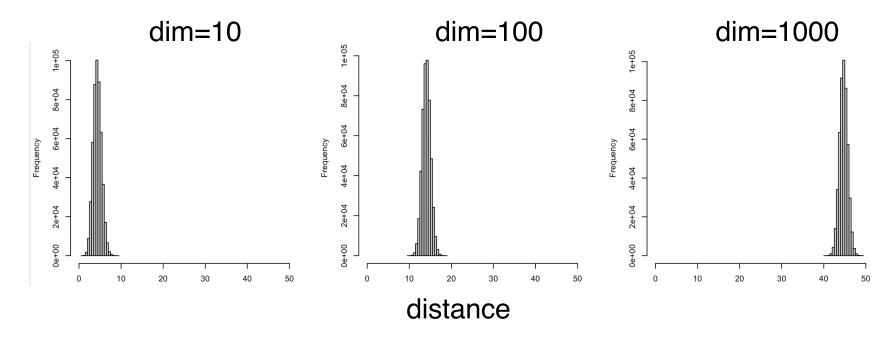


Dimension Reduction

Distances lose meaning at high dimensional space (curse of dimensionality)

$$\frac{D_{\max} - D_{\min}}{D_{\min}} \to 0.$$

Example: distance between points sampled from a normal distribution





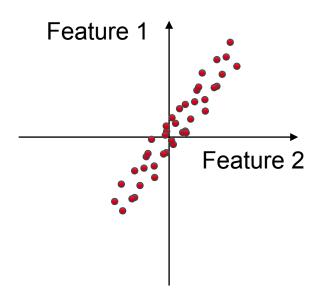
Dimension Reduction

- Distances lose meaning at high dimensional space (curse of dimensionality)
- Unspecific Filtering (without class labels):
 - Keep variables with highest variance (high variable genes)
 - Rationale: important features change values across groups
- Dimensionality Reduction by Transformation:
 - linear: principal component analysis (PCA)
 - Non-linear / manifold learning: t-SNE & UMAP (for visualisation)



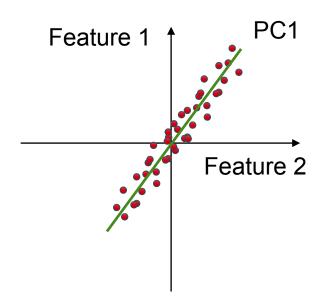
 For a data X, find linear combination of features (w) capturing most of data variance

$$\mathbf{w}_{(1)} = \underset{\|\mathbf{w}\|=1}{\text{arg max}} \{ \|\mathbf{X}\mathbf{w}\|^2 \}$$



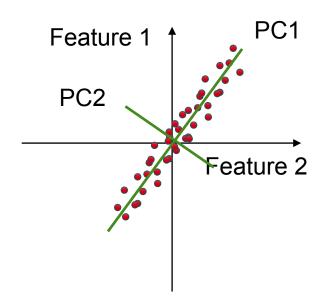
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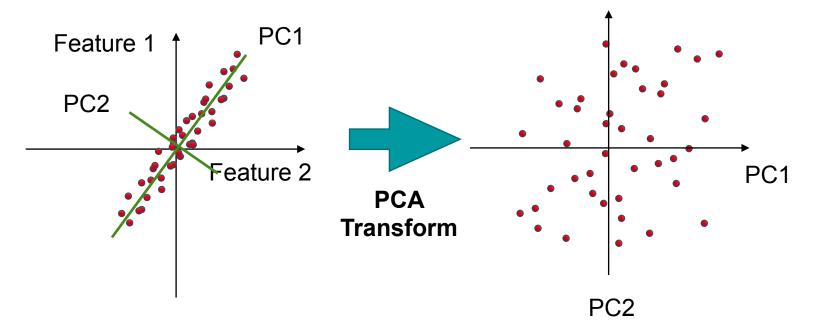
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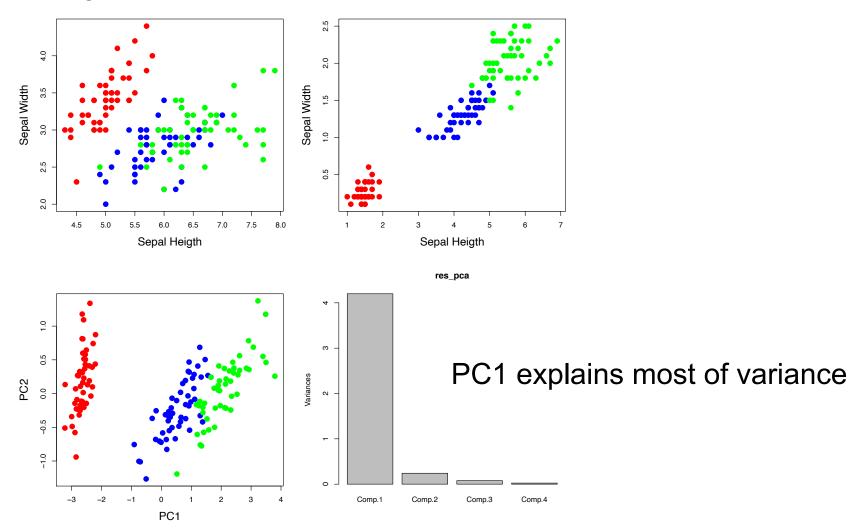
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PCA - Iris

Original iris data had 4 variables

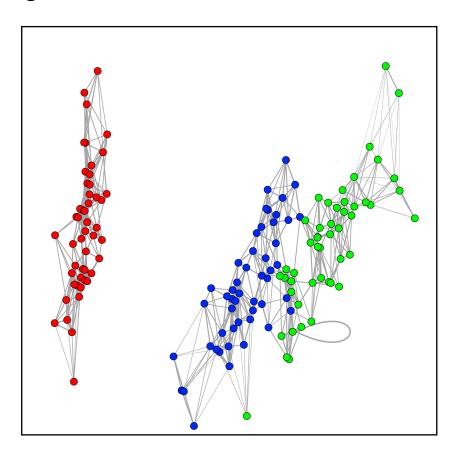




Clustering on PCA space

- For single cell data it is usually cluster in PCA space
 - · This is crucial for high-dimensional data!

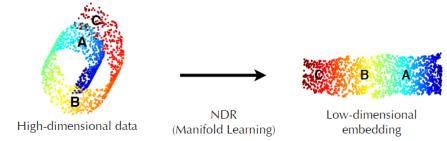
KNN graph of IRIS in PCA space



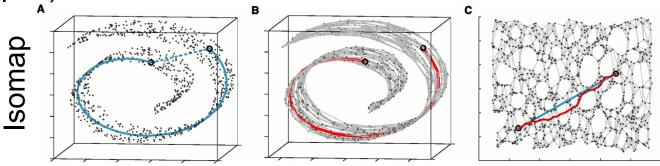


Non-linear / Manifold methods

 Data might be distributed at particular regions of a high dimensional space



Manifold methods use topological distance (nearest neighbour graphs)



t-SNE and UMAP are newer/widely used methods



t-distributed stochastic neighbor

For a given kernel D learn a I dimensional map Y

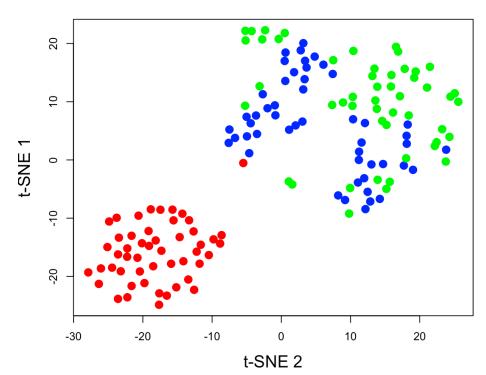
$$KL(D | Q) = \sum d_{ij}log(\frac{d_{ij}}{q_{ij}})$$
 where $q_{ij} = \frac{|y_i - y_j|^2}{\sum_k \sum_l |y_k - y_l|^2}$

t-distributed stochastic neighbor

For a given kernel D learn a I dimensional map Y

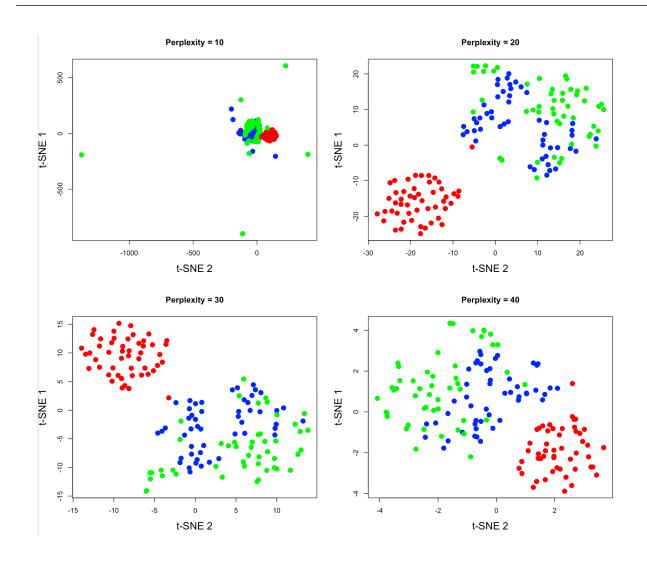
$$KL(D | Q) = \sum d_{ij}log(\frac{d_{ij}}{q_{ij}})$$
 where $q_{ij} = \frac{|y_i - y_j|^2}{\sum_k \sum_l |y_k - y_l|^2}$







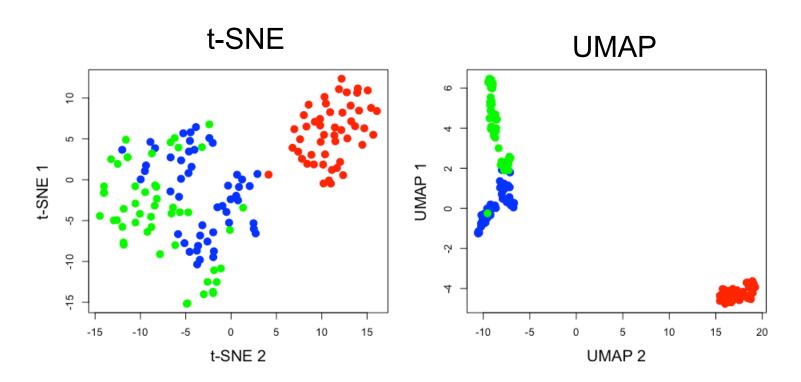
t-distributed stochastic neighbor



- Sensitive to distinct starts and parametrisation
 - Perplexity ~ neighbourhood size



Manifold learning and IRIS



- Nice low dimensional visualisation of the data
- Caution: These methods fail capturing global structures (distance between clusters!)

Resume / Dimension Reduction

- PCA analysis is a wide spread technique to reduce dimension!
 - Can only capture linear relationships
- Manifold methods
 - Nice low dimensional representation of data
 - Require parametrisation and lose global distance information

Complete course on manifolds/dimension reduction:

https://www.youtube.com/watch?v=evGm6lJKrDI&t=4421s



Cluster Validation

- How to evaluate clustering results? Which is the best method? How many clusters?
- Internal/relative validation:
 - Measure of cluster coherence:
 - Distance within a cluster -> small (compactness)
 - Distance between clusters -> high (separation)
 - Stability measures:
 - Cluster data in part of the data and compare results
- External validation:
 - Compare clusters with class labels (iris data)
 - Not possible in real word problems!



Silhouette - Internal Index

The silhouette for a given object *i* is defined as:

$$s(i) = \frac{b(i) - a(i)}{max(a(i), b(i))}$$

where

a(i) -mean distance of i to objects on same cluster (compactness) d(i,k) - mean distance of i to objects of cluster k (not own) $b(i) = min_k (d(i,k))$ (separation)

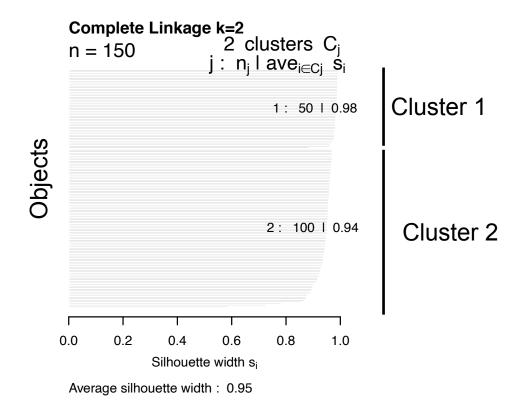
Average of s(i) -> quality of all results or clusters

Value of 1 indicate perfect solutions!



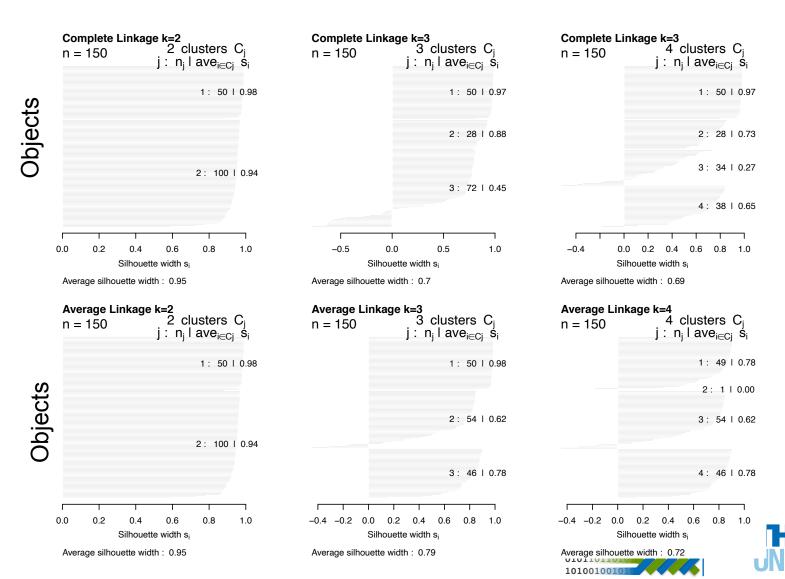
Silhouette - Internal Index / Iris

silhouette values for hierarchical clustering with Pearson



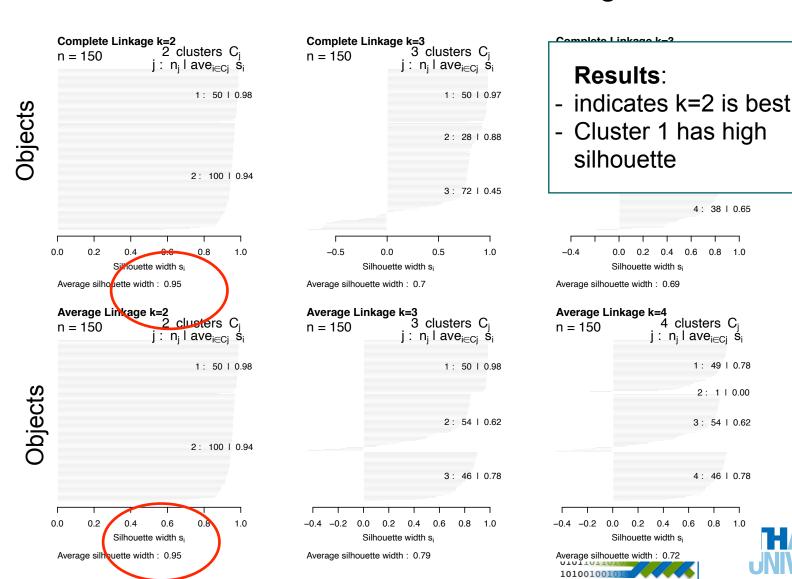
Silhouette - Internal Index / Iris

silhouette values for hierarchical clustering with Pearson



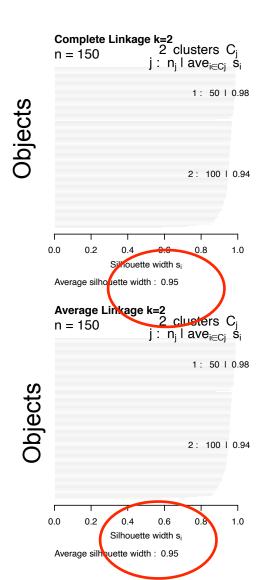
Silhouette - Internal Index / Iris

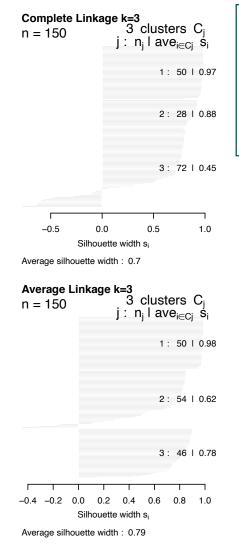
silhouette values for hierarchical clustering with Pearson



Silhouette - Internal Index / Iris

silhouette values for hierarchical clustering with Pearson



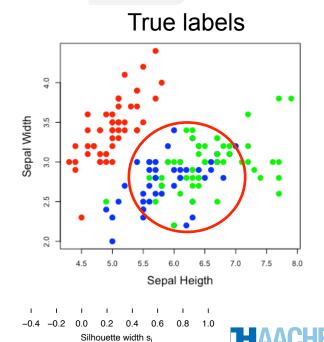


Results:

- indicates k=2 is best
- Cluster 1 has high silhouette

Average silhouette width: 0.72

1010010010



Gap statistic - Internal Index

For a given solution with *K clusters*

$$W_K = \sum_{k=1}^K \sum_{y_i = k} \sum_{y_j = k} ||x_i - x_j||^2$$

 W_K - measures cluster compactness

 W_K - tends to 0 for increasing K

The Gap Statistic consider clustering of random data W*

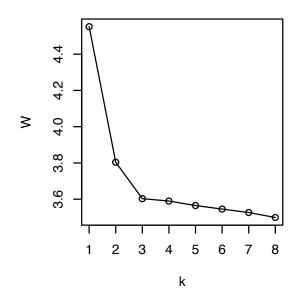
$$GAP(k) = E_r[logW_K^*] - logW_K$$

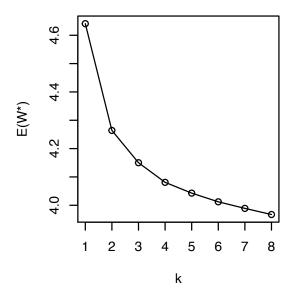
where *W** estimated from clustering random points at the same data space of *X*

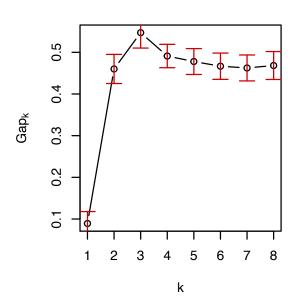


Gap statistic - Iris

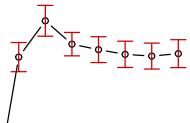
GAP statistics for Iris / Average Linkage with Pearson

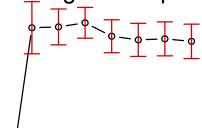


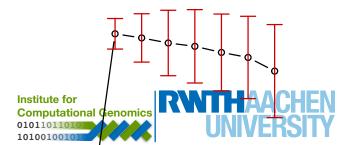




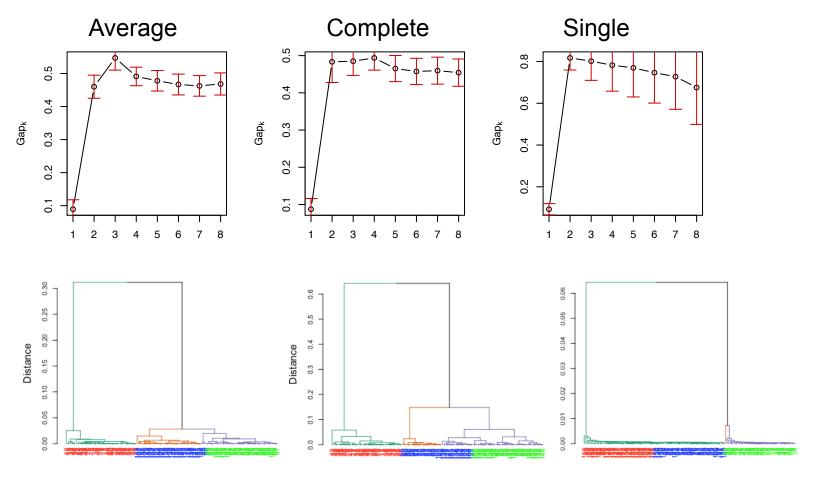
3 clusters has highest Gap !!!







GAP statistics for distinct linkage methods



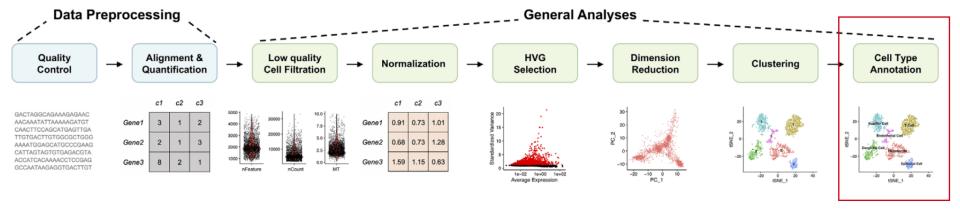


Resume / Validation

- Help detection of number of clusters / real clusters
 - Do not work perfectly!
- GAP statistics is widely used
 - Requires r data randomisations
 - high computational costs
 - random datasets uniformly distributed (unreal assumption)
- Expert interpretation is important!

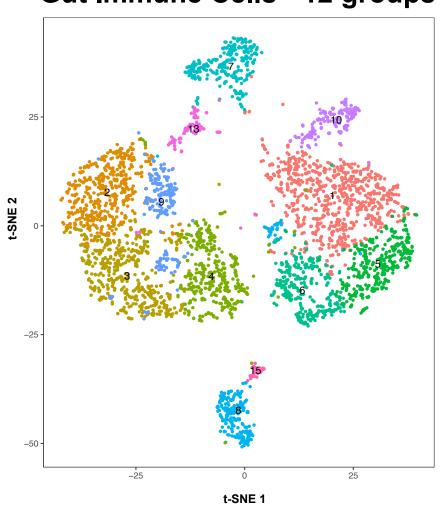


Basics Bioinformatics - single cell RNA-seq



Basics Bioinformatics - Clustering

Gut Immune Cells - 12 groups



Clustering - identify cells with similar expression patterns

- based on PCA (20 dimension)

How to identify cell types?



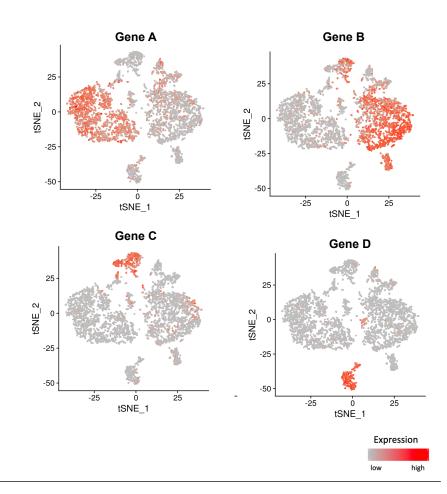
Cell Identity with an Expert

Gut Immune Cells - 12 groups

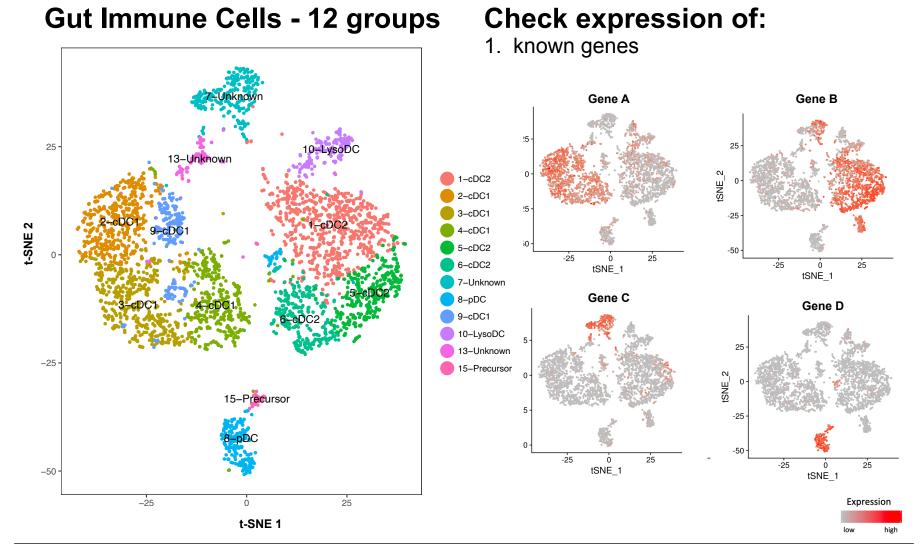
25 t-SNE 2 -25 -50 -25 t-SNE 1

Check expression of:

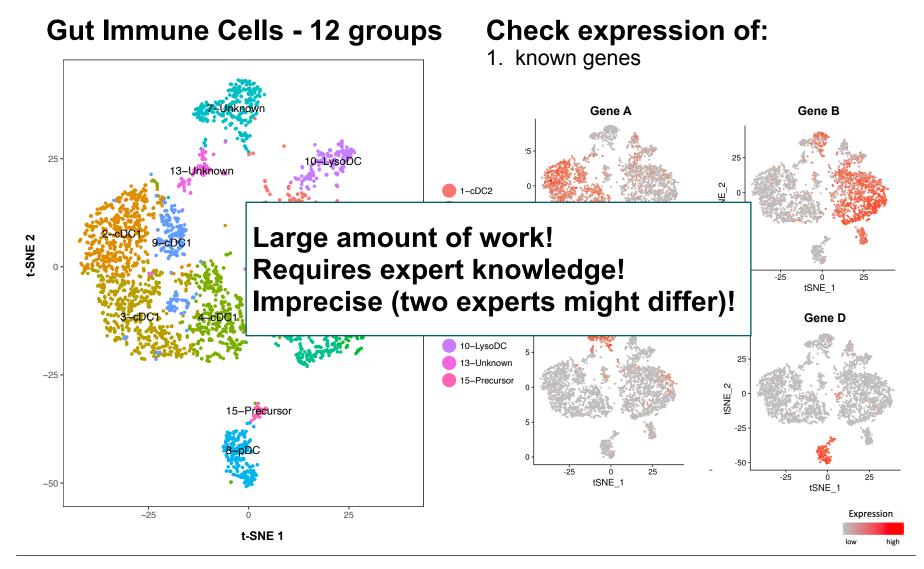
1. known genes



Cell Identity with an Expert



Cell Identity with an Expert



Resume / Single cell clustering

- Finding groups of single cells require complex pipeline:
 - Cell filtering
 - Normalisation
 - Artefact removal
 - Dimension reduction
 - Integration
 - Clustering
 - Cell annotation / visualisation
- Open points:
 - How to deal with large data sets (millions of cells)?
 - How to detect cells of rare populations?



Calendar

Today – Introduction to Bioinformatics, Next Generation Sequencing, Single cell Analysis

2.05.2022 - Single cell Analysis Practical

8.05.2022 – Computational Epigenomics / Project Description / Using RWTH HPC/GPU cluster

15.05.2022 - 4.7.2022 - Project development

11.07.2022 – Project Presentation

Communication/discord channel: https://discord.gg/



Thank you!

